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# Investigation of air flow near a mach number of one by the Schlieren Method.

Watkins, David Wayne, Jr.; Watkins, David Wayne

Massachusetts Institute of Technology

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INVESTIGATION OF AIR FLOW  
NEAR A MACH NUMBER OF ONE,  
BY THE SCHLIEREN METHOD

BY  
DAVID WAYNE WATKINS, JR.

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Cambridge, Massachusetts,  
June 3, 1946.

Professor George W. Swett,  
Secretary of the Faculty,  
Massachusetts Institute of Technology,  
77 Massachusetts Avenue,  
Cambridge, Massachusetts.

Dear Professor Swett:

Herewith I submit my thesis entitled, "Investigation  
of Air Flow Near a Mach Number of One, by the Schlieren  
Method" in partial fulfillment of the requirements for the  
degree of Master of Science in Aeronautical Engineering at  
the Massachusetts Institute of Technology.

Respectfully,

*David W. Watkins, Jr.*  
David W. Watkins, Jr.



Cambridge, Massachusetts,  
June 3, 1944.

Professor George A. Davis,  
Secretary of the Faculty,  
Massachusetts Institute of Technology,  
75 Massachusetts Avenue,  
Cambridge, Massachusetts.

Dear Professor Davis:

Herewith I submit a copy of a letter dated  
of air flow over a semi-circular airfoil, by the author  
written in partial fulfillment of the requirements for the  
degree of Master of Science in Aeronautical Engineering at  
the Massachusetts Institute of Technology.

Sincerely,  
David W. Johnston

David W. Johnston  
David W. Johnston, Jr.

100

INVESTIGATION OF AIR FLOW NEAR A MACH NUMBER OF ONE,  
BY THE SCHLIEREN METHOD

by

David Wayne Watkins, Jr.  
Lt. Comdr., U. S. Navy.

Submitted in Partial Fulfillment of the  
Requirements for the  
Degree of Master of Science  
in  
Aeronautical Engineering  
from the  
Massachusetts Institute of Technology  
1946

Signature of Author:

David W. Watkins, Jr.

Department of Aeronautical Engineering, June 1946.

Signature of Professor in Charge of  
Research:

Joseph H. Keenan

Signature of Chairman of Department  
Committee on Graduate Students:

C. S. Draper

INVESTIGATION OF THE PROGRESS OF THE WORK OF THE

IN THE DEPARTMENT OF AGRICULTURE

OF

THE DEPARTMENT OF AGRICULTURE  
WASHINGTON, D. C.

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1920

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Department of Agricultural Investigation, June 1920.

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Signature of subject:  
Department of Agricultural Investigation, June 1920.  
Signature of Professor in Charge of  
Department  
Signature of Director of Department  
Signature of Professor in Charge of

### ACKNOWLEDGMENTS.

It is with pleasure that I acknowledge my indebtedness to Professor J. H. Keenan, who suggested the thesis problem and the possible lines of attack, and helped me constantly through conference on the many difficulties I encountered. Mr. E. P. Neumann also gave freely of his time and offered many valuable suggestions, especially in connection with the investigation of the boundary layer. Mr. A. H. Shapiro suggested an explanation of the multiple shocks observed. Mr. F. Lustwerk explained the use of the Schlieren equipment, and helped with collateral reading. Professor H. E. Edgerton lent his high speed movie equipment, explained its use, and aided me in the development of the film. Mr. Charles Wyckoff gave many days of his time operating the movie equipment. The personnel of the Boston Naval Shipyard permitted free use of their photographic laboratory and helped me with printing the pictures.



EXHIBIT

It is also possible that I am overlooking an investigation by Professor J. H. Brown, who suggested the film problem and the possible lines of attack, and helped me considerably through cooperation on the way difficulties I encountered. Mr. J. H. Brown also gave credit to his film and offered many valuable suggestions, especially in connection with the investigation of the possible impact. Mr. J. H. Brown was greatly an explanation of the entire scene observed. Mr. J. H. Brown explained the use of the Holston system, and helped with various details. Professor J. H. Brown also gave credit to his movie company, explained the use, and also as to the development of the film. Mr. Brown spent some many days of his time operating the movie equipment. The personnel of the Brown Hotel Company provided free use of their photographic laboratory and helped me with printing the pictures.

## TABLE OF CONTENTS.

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- II. Introduction.
- III. Apparatus and Procedure.
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- V. Discussion of Results.
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### SUMMARY.

The problem investigated was the manner of dissipation of shocks in air flowing through a nozzle. The shocks observed were oblique shocks. They were formed by decreasing the back pressure on the nozzle exit by means of an ejector. The mouth of the nozzle was open to laboratory air. The back pressure was increased after the shocks were formed by closing the valve between the nozzle exit and the ejector, causing dissipation of the shocks. The phenomena were observed by means of a high speed movie camera. The results indicated that the shocks formed dissipated in the throat of the nozzle. They were never observed upstream from the throat.



## INTRODUCTION.

In a Schlieren study of two dimensional ejectors, Mr. F. Lustwerk noted the appearance of a sharp fronted disturbance in the subsonic secondary stream under certain conditions. It was desired to know how long the secondary stream could support this disturbance and the manner of its dissipation.

It was decided to simplify the problem by removing the primary stream from the ejector; that is, to investigate the dissipation of a shock in a two dimensional nozzle. This was done to reduce the number of variables involved, so that some results could be obtained in the allotted time.

To attack this problem, it was decided to set up a convergent-divergent nozzle which was supplied by opening the mouth of the nozzle to the atmosphere, to keep entering turbulence as low as possible, and to supply the necessary controlled pressure drop by means of an ejector and suitable valves. Then the phenomena related to the dissipation of the shocks formed in the nozzle could be observed through a Schlieren optical system and recorded on a photographic medium. A few single flash pictures were taken to ascertain that there were dynamic effects to be observed. Then high speed movies were taken of these effects.



It is interesting to note that the same type of  
 evidence is also found in the case of the  
 ... it was found to be the same as the  
 ... the same as the ...

It was decided to study the problem of removing the primary stress from the speaker; that is, to investigate the elimination of a stress in a two-dimensional system. This was done by taking the number of variables involved in that same system as contained in the affected time. To stress this problem, it was decided to set up a two-variable-dimension system which was supplied by opening the mouth of the mouth in the atmosphere, to keep constant the pressure as low as possible, and to supply the necessary controlled pressure from a source of an electric and magnetic valves. Then the phenomenon related to the elimination of the stress formed in the mouth would be observed through a controlled optical system and recorded on a photographic medium. A few studies have shown that there is a certain amount of stress in the mouth as it is observed. This has been shown to be a two-dimensional system.

## APPARATUS.

The major piece of equipment used in this investigation was a double pass Schlieren optical system. Fig. 1 is a sketch of this apparatus, and a more complete description and discussion of it is given in the Appendix.

The nozzle used was a convergent-divergent two dimensional nozzle made of mild steel, with glass end walls. The nozzle was one-half inch wide and for a distance of one-half inch was parallel to the longitudinal axis of the nozzle. The entry to the throat consisted of the arcs of two circles of six inch radii, and extended about three and one-half inches along the longitudinal axis. (See Fig. 2.) The divergent portion of the nozzle consisted of two planes placed at a four degree slope away from the longitudinal axis. The corner between the throat section and the divergent section was carefully blended to destroy the sharp corner. Fig. 3 is a drawing of the frame used to mount the test section. Fig. 4 is a sketch of the nozzle assembly as it was used. The glass walls of the nozzle were made of high grade optical glass, and the surfaces were ground optically flat and parallel.

To take the pictures shown in the results, a standard "Edgerton type", high speed, thirty-five millimeter movie camera was used with an air gap spark substituted for the Edgerton flash tube as a light source. The Appendix fully describes this apparatus and Fig. 5 is a schematic wiring diagram of the light source.



## APPENDIX

The major part of the investigation was in this investigation  
was a large scale examination of the system of this apparatus, and a more complete description  
and discussion of it is given in the Appendix.  
The results show that a convenient-divided two sided-  
electrical system made of mild steel, with glass and water. The  
results are one-half inch wide and for a distance of one-half  
inch are parallel to the longitudinal axis of the nozzle.  
The only in the largest diameter of the area of two circles  
of six inch width, and extending about three and one-half  
inches along the longitudinal axis. (See Fig. 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 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2012, 2013, 2014, 2015, 2016, 2017, 2018, 2019, 2020, 2021, 2022, 2023, 2024, 2025, 2026, 2027, 2028, 2029, 2030, 2031, 2032, 2033, 2034, 2035, 2036, 2037, 2038, 2039, 2040, 2041, 2042, 2043, 2044, 2045, 2046, 2047, 2048, 2049, 2050, 2051, 2052, 2053, 2054, 2055, 2056, 2057, 2058, 2059, 2060, 2061, 2062, 2063, 2064, 2065, 2066, 2067, 2068, 2069, 2070, 2071, 2072, 2073, 2074, 2075, 2076, 2077, 2078, 2079, 2080, 2081, 2082, 2083, 2084, 2085, 2086, 2087, 2088, 2089, 2090, 2091, 2092, 2093, 2094, 2095, 2096, 2097, 2098, 2099, 2100, 2101, 2102, 2103, 2104, 2105, 2106, 2107, 2108, 2109, 2110, 2111, 2112, 2113, 2114, 2115, 2116, 2117, 2118, 2119, 2120, 2121, 2122, 2123, 2124, 2125, 2126, 2127, 2128, 2129, 2130, 2131, 2132, 2133, 2134, 2135, 2136, 2137, 2138, 2139, 2140, 2141, 2142, 2143, 2144, 2145, 2146, 2147, 2148, 2149, 2150, 2151, 2152, 2153, 2154, 2155, 2156, 2157, 2158, 2159, 2160, 2161, 2162, 2163, 2164, 2165, 2166, 2167, 2168, 2169, 2170, 2171, 2172, 2173, 2174, 2175, 2176, 2177, 2178, 2179, 2180, 2181, 2182, 2183, 2184, 2185, 2186, 2187, 2188, 2189, 2190, 2191, 2192, 2193, 2194, 2195, 2196, 2197, 2198, 2199, 2200, 2201, 2202, 2203, 2204, 2205, 2206, 2207, 2208, 2209, 2210, 2211, 2212, 2213, 2214,

The film used was Eastman Kodak Company's "Super XI", developed for maximum contrast in the same Company's standard developer "D-11" for sixteen minutes. For further discussion of the photography methods see the Appendix.

The required pressure difference across the nozzle was obtained by reducing the downstream pressure from atmosphere by means of an ejector.

The flow of air was from atmosphere, through the test section, suitable piping, a butterfly valve, a silencer, and a globe valve to the secondary stream of the ejector.

In taking a high speed series of pictures, the following procedure was used. The pressure difference across the nozzle was adjusted by use of the globe valve, until a shock was observed in the aperture of the camera. The general illumination in the laboratory was switched off, and the camera was started. The butterfly valve, which was spring loaded to the wide open position, was manually closed. Next, it was allowed to open fully. This valve cycle was repeated two or three times during the exposure of a hundred feet of film. The film speed through the camera averaged about fifty feet per second. This made the time interval between exposures about one five-hundredth of a second. The exposure time of each exposure was about five microseconds.



The film used was Kodak's "Super 8",

developed for sixteen minutes in Kodak D-19.

One exposure "8-11" for sixteen minutes. For further

development of the photographic method see the appendix.

The positive prints of the film were

and obtained by running the film through a

negative of each of the prints.

The film of the two exposures, through the first

section, was a single strip, a relatively wide, a

and a single strip to the secondary section of the strip.

In each of the two sections of film, the

and procedure was used. The procedure differed from the

results are obtained by one of the film strips, until a

was obtained in the exposure of the film. The second

impression in the laboratory was exposed 10, and the

was similar. The strip of film, which was

in the film strip, was relatively small. But, it

allowed to open this. This film strip was

three times longer the exposure of a

The film strip through the camera

per second. This was the film

about the five-minute of a

and exposure was about five

## RESULTS.

The results are presented as pictures in Figs. 6 through 32. They are selected series of enlargements made from one of the hundred foot lengths of exposures made in the high speed camera. The whole length contains about twelve hundred exposures, many of which would be of no interest. In selecting the pictures to be presented, an attempt was made to select those demonstrating most clearly the phenomena occurring in the fewest number of exposures. Since time was an element of interest in the investigation, the continuity of each series was maintained; that is, within each series, the pictures presented follow each other in sequence, with a time interval between pictures of one five-hundredth of a second. The boundary layer group of pictures are an exception to this in that they were of necessity made on another strip of film and were isolated selections and not a continuous series.

Figs. 6 through 13 are one series. This series demonstrates the nature of the multiple shocks at a pressure ratio somewhat below critical, and are from a section of the film in which no change was occurring in the back pressure. They show clearly the oscillations of the shocks occurring in the "steady state" condition.

Figs. 14 through 18 show the manner of dissipation of the shocks with increasing pressure ratio.

Figs. 19 through 27 show the manner of formation of the shock with decreasing pressure ratio.



RESULTS

The results are presented in Figures 1 through 5. Figure 1 shows the results of the first series of experiments. The results of the second series are shown in Figure 2. The results of the third series are shown in Figure 3. The results of the fourth series are shown in Figure 4. The results of the fifth series are shown in Figure 5. The results of the sixth series are shown in Figure 6. The results of the seventh series are shown in Figure 7. The results of the eighth series are shown in Figure 8. The results of the ninth series are shown in Figure 9. The results of the tenth series are shown in Figure 10. The results of the eleventh series are shown in Figure 11. The results of the twelfth series are shown in Figure 12. The results of the thirteenth series are shown in Figure 13. The results of the fourteenth series are shown in Figure 14. The results of the fifteenth series are shown in Figure 15. The results of the sixteenth series are shown in Figure 16. The results of the seventeenth series are shown in Figure 17. The results of the eighteenth series are shown in Figure 18. The results of the nineteenth series are shown in Figure 19. The results of the twentieth series are shown in Figure 20. The results of the twenty-first series are shown in Figure 21. The results of the twenty-second series are shown in Figure 22. The results of the twenty-third series are shown in Figure 23. The results of the twenty-fourth series are shown in Figure 24. The results of the twenty-fifth series are shown in Figure 25. The results of the twenty-sixth series are shown in Figure 26. The results of the twenty-seventh series are shown in Figure 27. The results of the twenty-eighth series are shown in Figure 28. The results of the twenty-ninth series are shown in Figure 29. The results of the thirtieth series are shown in Figure 30. The results of the thirty-first series are shown in Figure 31. The results of the thirty-second series are shown in Figure 32. The results of the thirty-third series are shown in Figure 33. The results of the thirty-fourth series are shown in Figure 34. The results of the thirty-fifth series are shown in Figure 35. The results of the thirty-sixth series are shown in Figure 36. The results of the thirty-seventh series are shown in Figure 37. The results of the thirty-eighth series are shown in Figure 38. The results of the thirty-ninth series are shown in Figure 39. The results of the fortieth series are shown in Figure 40. The results of the forty-first series are shown in Figure 41. The results of the forty-second series are shown in Figure 42. The results of the forty-third series are shown in Figure 43. The results of the forty-fourth series are shown in Figure 44. The results of the forty-fifth series are shown in Figure 45. The results of the forty-sixth series are shown in Figure 46. The results of the forty-seventh series are shown in Figure 47. The results of the forty-eighth series are shown in Figure 48. The results of the forty-ninth series are shown in Figure 49. The results of the fiftieth series are shown in Figure 50. The results of the fifty-first series are shown in Figure 51. The results of the fifty-second series are shown in Figure 52. The results of the fifty-third series are shown in Figure 53. The results of the fifty-fourth series are shown in Figure 54. The results of the fifty-fifth series are shown in Figure 55. The results of the fifty-sixth series are shown in Figure 56. The results of the fifty-seventh series are shown in Figure 57. The results of the fifty-eighth series are shown in Figure 58. The results of the fifty-ninth series are shown in Figure 59. The results of the sixtieth series are shown in Figure 60. The results of the sixty-first series are shown in Figure 61. The results of the sixty-second series are shown in Figure 62. The results of the sixty-third series are shown in Figure 63. The results of the sixty-fourth series are shown in Figure 64. The results of the sixty-fifth series are shown in Figure 65. The results of the sixty-sixth series are shown in Figure 66. The results of the sixty-seventh series are shown in Figure 67. The results of the sixty-eighth series are shown in Figure 68. The results of the sixty-ninth series are shown in Figure 69. The results of the seventieth series are shown in Figure 70. The results of the seventy-first series are shown in Figure 71. The results of the seventy-second series are shown in Figure 72. The results of the seventy-third series are shown in Figure 73. The results of the seventy-fourth series are shown in Figure 74. The results of the seventy-fifth series are shown in Figure 75. The results of the seventy-sixth series are shown in Figure 76. The results of the seventy-seventh series are shown in Figure 77. The results of the seventy-eighth series are shown in Figure 78. The results of the seventy-ninth series are shown in Figure 79. The results of the eightieth series are shown in Figure 80. The results of the eighty-first series are shown in Figure 81. The results of the eighty-second series are shown in Figure 82. The results of the eighty-third series are shown in Figure 83. The results of the eighty-fourth series are shown in Figure 84. The results of the eighty-fifth series are shown in Figure 85. The results of the eighty-sixth series are shown in Figure 86. The results of the eighty-seventh series are shown in Figure 87. The results of the eighty-eighth series are shown in Figure 88. The results of the eighty-ninth series are shown in Figure 89. The results of the ninetieth series are shown in Figure 90. The results of the ninety-first series are shown in Figure 91. The results of the ninety-second series are shown in Figure 92. The results of the ninety-third series are shown in Figure 93. The results of the ninety-fourth series are shown in Figure 94. The results of the ninety-fifth series are shown in Figure 95. The results of the ninety-sixth series are shown in Figure 96. The results of the ninety-seventh series are shown in Figure 97. The results of the ninety-eighth series are shown in Figure 98. The results of the ninety-ninth series are shown in Figure 99. The results of the hundredth series are shown in Figure 100.

E

Figs. 28 through 32 are the pictures of the boundary layer, selected to show variations in pressure ratio from below critical to one.

It should be noted that no attempts have been made to obtain quantitative results because such results, using a double pass Schlieren optical system, are extremely difficult to obtain.

The disturbance which may be noted on one side of the nozzle throat of all pictures was caused by a small nick in the corner of the nozzle half. This nick was about .01 inches deep by .01 inches across and about one-eighth of an inch long.

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1  
The 30 strong 12 are the children of the country  
they, believed to have been in previous years  
below which is one.

It should be noted that no attempt has been made to  
obtain quantitative results because such results, being a  
double test method optical system, are extremely difficult  
only as optical.

The distance which may be noted on one side of the  
results shows that all systems are noted by a small side in  
the center of the results only. This side was about 101  
less than 101. 101 less than 101 and about one-eighth of an  
inch less.

The results of the 101 less than 101 and about one-eighth of an  
inch less, are shown in the following table. The results of the  
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101 less than 101 and about one-eighth of an inch less, are shown  
in the following table. The results of the 101 less than 101 and  
about one-eighth of an inch less, are shown in the following table.



## DISCUSSION OF RESULTS.

As can be seen in Fig. 6, the change from supersonic flow in the throat to subsonic flow downstream of the throat occurred through a multiple shock. Taking Fig. 10 as an example, and considering the occurrences in the direction of flow: the velocity increases through the throat section. Just behind the throat, a region of compression occurs which is thicker in the center of the flow area and decreases to a point before reaching the nozzle boundary, thus indicating the presence of a boundary layer. The downstream side of this region is flat. Next downstream is a region of expansion which appears to be a mirror image of the compression region. At the centerline, the expansion region grades into another compression. Away from the centerline and between the first expansion and the following compression, lies a wedge shaped constant flow region. Following the second compression the above described phenomena appear cyclically.

It appears that other photographs contain the same type of compression-expansion waves though not so symmetrically arranged, and the outer ends of the upstream side of the compressions are seldom so clearly bent downstream from the centerline of the nozzle.

Figs. 14 through 18 show the dissipation of these shocks. They move into the throat and weaken in intensity. They were never observed upstream of the throat section.

## DESCRIPTION OF RESULTS

As can be seen in Fig. 2, the diagram shows approximately  
flow in the lower to moderate flow conditions of the lower  
portion through a multiple system. During this, it is an  
example, and illustrating the conditions in the direction of  
flow. The velocity increases through the throat section.  
This being the case, a region of expansion occurs which  
is visible in the center of the flow area and decreases to a  
point before reaching the nozzle boundary, thus indicating  
the presence of a boundary layer. The downstream side of  
this region is flat. Most downstream is a region of expansion  
also which appears to be a limit limit of the expansion  
region. At the centerline, the expansion region extends into  
another expansion. Away from the axis, the expansion and between  
the first expansion and the following expansion, there is  
a region which contains flow region. Following the second ex-  
pansion the flow is disturbed throughout the entire section.  
It appears that other conditions contain the same type  
of expansion-expansion region though not so symmetrically  
arranged, and the outer edge of the expansion side of the  
expansion is also an edge of the flow boundary from the  
centerline of the nozzle.

Fig. 3 shows the flow in the direction of flow  
which. They have been the same and appear to be identical.  
They have been the same and appear to be identical.



This would indicate that the subsonic stream will not support this type of shock over any considerable distance, if at all.

Since other shocks have been observed in a subsonic stream, as was mentioned in the Introduction, the question of the mechanism of the shocks observed becomes paramount. Two attacks are possible; one is to start with the hypothesis that the compression shock forms itself in midstream. Then by observing closely Figs. 28 through 32, which are photographs of the boundary layer, slight waves in the boundary layer can be detected. The key to the nature of the shocks lies in the relation of these waves to the shocks. Considering the boundary layer as a region of constant pressure, the reflection of the compression shock is a "Prandtl-Meyer expansion wedge". As has been noted, an expansion exists after the compression shock. Then the next compression-expansion series follows since supersonic flow may exist out of the first expansion. This process is repeated until finally subsonic flow is attained from the last expansion wedge. There is no apparent relation between one shock (compression and expansion) and the cycle following it.

The weakness in this explanation lies in the hypothesized compression shocks which must start in midstream.

If, on the other hand, consideration is first taken of the boundary layer, which is evidently rather thick, then the following explanation may be made. Slight variations in

This would indicate that the system will not run  
past this type of about every 1000 miles. It  
is all.

Since other rocks have been observed in a sequence  
stream, as was mentioned in the introduction, the position  
of the boundary of the system appears to be permanent.

The other two possibilities are: one is to start with the type-  
trials that the compression about 1000 miles is constant.

Then by observing closely the 1000 miles, we can see  
phenomena at the boundary layer, which occur in the form-

but layer can be detected. The key to the nature of the

which lies in the relation of these waves to the rocks.

Considering the boundary layer as a region of constant pres-  
sure, the relation of the compression about 1000 miles is a "boundary-

layer expansion wedge". It has been noted, an expansion

exists after the compression about 1000 miles. Then the first compression-

expansion wedge follows after compression. This wedge will exist one

of the first expansion. This process is repeated until finally

boundary flow is repeated from the last expansion wedge. These

is an apparent relation between one expansion wedge and the

general) and the order following it.

The sequence in this expansion lies in the opposite

and compression about 1000 miles that is observed.

It, on the other hand, considering is first layer of

the boundary layer, which is a boundary layer, then

the following expansion may be seen. Since variation in



the thickness of the boundary layer caused by local oscillations in velocity and pressure such as have been found on investigating the boundary layer of a flat plate (Ref. 3) lead to the conclusion that a convex boundary layer surface may exist. If it is further assumed that the flow in the stream attempts to follow these fluctuations in the boundary layer thickness, then the situation as described in Ref. 4 exists. That is, the flow along a curved boundary is continuous as long as the radii vectors drawn at Machs angles from any point on the boundary do not intersect. When the boundary reaches a sufficient degree of concavity, the radii vectors do intersect and a region of discontinuous flow results. The compression wave thus formed would occur slightly downstream of the concavity in the boundary layer which caused it, thus causing a region of higher pressure at a point where the tendency of the boundary layer is to expand. To equalize the pressure, the boundary layer contracts causing an expansion of the free stream greater than the nozzle walls indicate. The turning of the free stream causes a further depression of the boundary layer which is attempting to expand with the decreasing pressure gradient. As the stream is deflected from the boundary layer a concavity in the boundary layer occurs causing the following compression shock and another cycle of the above mechanism, and so on until subsonic flow results.





In either explanation posed above, each of the multiple shocks would be oblique, not a plane compression shock, and the exit velocity of the stream may be either supersonic or subsonic. In the first explanation posed above, a shock similar to the "hypothesized" shock has been observed in Schlieren pictures of flow around an airfoil taken at the Guggenheim Laboratory at California Institute of Technology. This shock generally slants upstream from the boundary layer and does not lie along a straight line. In the second explanation above, assuming the mean surface of the boundary layer is parallel to the nozzle walls, the shock must slant downstream from the boundary layer, though not necessarily along a straight line. However, if the mean surface of the boundary layer diverges enough from the nozzle walls, then the shock might well slant upstream from the boundary layer. The results of this investigation show no conclusive evidence that the shocks bend in either direction. Also, there is no accurate correlation between any one shock and the boundary layer adjoining it. Hence, no definite conclusion can be reached as to the relation between the waves in the boundary layer and the multiple shocks, except that they both exist at the condition of maximum flow through the nozzle.

The dissipation of these shocks, as may be observed in Figs. 14 through 18, occurs as a weakening of the com-

[illegible]

The situation of the country, as far as the situation of the country is concerned, is as follows:



pression region and a movement upstream into the throat of the nozzle. Apparently the cause of the shocks must move upstream and its intensity must decrease. Since the velocity of the free stream decreases, any cause of the shocks lying in the free stream might be expected to move upstream, but once this motion has started, it would be expected that the motion of the cause of the shocks would not stop at the throat or any other particular point.

On the other hand, if the position of the cause of the shocks is a function of the ratio of the mean boundary layer velocity to the mean free stream velocity, the shocks could conceivably move to a point where this function is again satisfied.

With supersonic flow it is difficult to visualize how a shock caused by free stream disturbances can do anything but move downstream at a velocity equal to the difference between the local sonic velocity and the velocity of the free stream. Figs. 6 through 13 show, however, that a compression wave may be traced from one figure to the next and that the motion of individual shocks may be traced going downstream, then reversing and moving upstream. The rate of change of this motion is about two hundred cycles per second. The region of this oscillation is from the downstream side of the throat section to about one throat diameter downstream of this point.



position (which was a constant distance from the origin  
of the system). Apparently the source of the waves must  
have remained at the same distance from the origin. Since the  
velocity of the wave is constant, any wave of the  
system is in the same phase as the wave which is  
reflected, and when this wave is reflected, it would be re-  
flected back the same of the same of the same and not  
stop at the point of any other position point.

On the other hand, if the position of the source of the  
waves is a function of the time of the wave, the wave  
velocity is not then the same velocity, and the wave  
consequently move to a point where this function is again  
reflected.

With reference to the fact that the wave is  
shock caused by the wave which is the source of the  
wave, the wave is a velocity equal to the distance between  
the total wave velocity and the velocity of the wave system.  
The wave is a wave, however, that a wave is a wave  
and the wave is a wave and the wave is a wave and the wave  
of the wave is a wave and the wave is a wave and the wave  
reflected and moving system. The wave of the wave of this  
moving is a wave and the wave is a wave and the wave  
of this reflection is a wave and the wave is a wave and the wave  
moving is a wave and the wave is a wave and the wave is a wave.

It is rather easy to visualize this condition when the upstream variation in the thickness of the boundary has a motion of the same frequency. As described in Ref. 4, this oscillation of boundary layer velocity and pressure actually exists on a flat plate in a subsonic stream and hence may be supposed to occur on the surface of the nozzle in a supersonic stream.

It was noted that when the shock was not too far downstream of the throat, but was in existence, a swishing sound could be heard issuing from the nozzle. As the back pressure was decreased and the shock moved further downstream, the sound decreased in frequency and intensity until it could not be heard.

It was further noted that with the maximum pressure difference obtainable across the nozzle the nature of the shock changed slowly with time. When the full pressure drop was attained by opening the valves controlling the flow through the nozzle, the shock appearing on the screen appeared similar to that shown in Figs. 26 and 27. After about forty-five seconds to a minute, this shock would have disappeared and in its place could be seen the multiple shocks similar to Fig. 8 and usually well downstream of the throat. The nature of this slow change was not observed. If the flow was instantaneously interrupted, the single shock of Fig. 27 would again appear.



It is rather easy to identify this condition when the upstream variation in the thickness of the boundary and a motion of the same thickness. As described in Fig. 4, this condition of boundary layer velocity and pressure actually exists on a flat plate in a turbulent stream and hence may be employed to study on the surface of the plate is a turbulent stream.

It was noted that when the flow was not too far downstream of the plate, the flow was in a state of a turbulent flow could be best found from the results. As the flow distance was increased and the back flow region was increased, the flow decreased in thickness and intensity and all it could not be found.

It was further noted that with the maximum pressure difference gradually across the plate the nature of the flow changed slowly with time. When the full pressure drop was applied to operate the valve controlling the flow through the nozzle, the flow changed on the surface appeared similar to that seen in Fig. 4. After about forty-five seconds to a minute, the flow would have disappeared and in the same time the flow would have changed similar to Fig. 4 and usually well downstream of the plate. The nature of this flow change was not constant. If the flow was instantaneously interrupted, the change state of Fig. 4 would occur again.

Professor Keenan has suggested that this may be a temperature effect. The stream being cooler than the surroundings would in time cool the walls of the nozzle and the stream itself would increase in velocity due to the heat absorbed by the stream. As the walls of the nozzle cooled, less heat would be transmitted to the stream, thus decreasing the velocity, and hence the strength of the shock, permitting the multiple shocks to form.

As can be clearly seen in Figs. 25, 26 and 27, a condensation shock was observed. This shock was annoying in that it blanked out some pictures that might otherwise have been of interest. However, its position in relation to the throat remained fairly constant and was generally downstream of the multiple oblique shocks when the pressure ratio across the nozzle was near critical. It is mentioned by way of explanation of the darkened region towards the nozzle exit. It is not felt that this condensation shock had any marked effects on the results. A more complete discussion of condensation shocks may be found in Ref. 7.

The results presented are far from conclusive as to the manner of dissipation of the shocks, as to the nature of the shocks themselves, and as to the relation between the boundary layer and the shocks. It would have been interesting, had time permitted, to find the relation between the boundary layer and the shocks. This could have been



the boundary lines and the whole. This could have been  
foreseen, but was pointed out in the relation between  
the boundary lines and the whole. It would have been in-  
of the whole (relative) and also the relation between  
the system of relations of the whole, as the whole  
The whole presented the two conditions as to  
relation of conditions which may be found in art. 7.  
and are related either to the whole. A more complete dis-  
whole is. It is not left that this nomination should  
of any of application of the law of the whole to the  
into which the whole was then divided. It is mentioned  
government of the whole which shows when the government  
to the whole (relative) and the whole and the whole  
and then of interest. However, the position in relation  
that it should not have relative but right of relation  
position must be observed. This must be stated in  
it can be directly seen in art. 22, 23 and 24, a new  
of the whole, relating the whole to the whole.  
system, that showing the whole, and hence the system  
whole could, then have been the relation in the  
the whole showed by the whole. In the whole of the  
and the whole itself would increase in relation and so  
necessarily with it. In fact, the whole of the whole  
dependence effect. The system of the whole and the  
position could be seen in art. 22, 23 and 24, a new



done by taking a run similar to those made with an angle of forty-five degrees between the nozzle axis and the Schlieren knife edge. Correlation of such a set of pictures with those obtained could have been much more informative than the results obtained.



### CONCLUSIONS.

1. The oblique shock observed in this investigation dissipates very quickly or never exists in a subsonic stream.

2. The results indicate that there is a close correlation between the boundary layer and the oblique shocks existing.

3. The noise issuing from the mouth of the nozzle, at pressure ratios slightly below critical, is caused by oscillation of the shock in "steady state".

4. The condensation shock presents no problem in this type of investigation since it occurs downstream of the effects observed.

5. Two distinct types of dynamic change occur under the conditions investigated; namely, a high speed oscillation of the multiple shocks, and a relatively slow change from a plane compression shock to the multiple shocks. Both effects occur with no change in the pressure ratio across the nozzle.

## Conclusions

1. The elliptical model assumed in this investigation of the elliptical model is not a realistic one.
2. The elliptical model is not a realistic one.
3. The elliptical model is not a realistic one.
4. The elliptical model is not a realistic one.
5. The elliptical model is not a realistic one.
6. The elliptical model is not a realistic one.
7. The elliptical model is not a realistic one.
8. The elliptical model is not a realistic one.
9. The elliptical model is not a realistic one.
10. The elliptical model is not a realistic one.



### RECOMMENDATIONS.

A quantitative Schlieren investigation of the relation between the boundary layer and the shocks in a supersonic stream might lend much light on the formation and dissipation shocks.

CONCLUSIONS

A comparative analysis of the relationship between the boundary layer and the shock in a supersonic stream shows that the formation of a shock wave is not dissipationless.

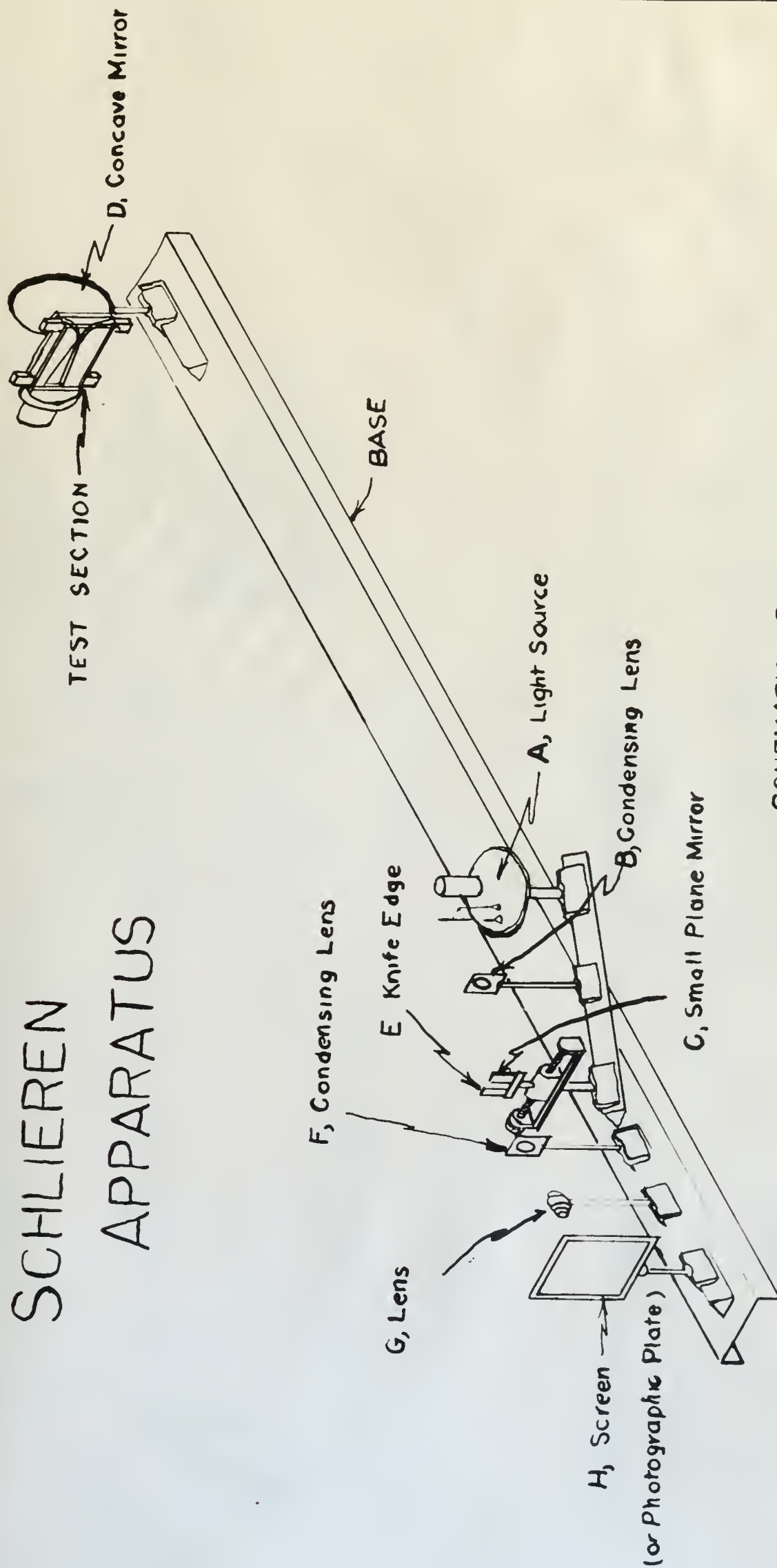
The results of the calculations show that the shock wave is a dissipative process and that the entropy increases across it.

The calculations also show that the shock wave is a discontinuity in the flow field and that the properties of the gas change abruptly across it.

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The calculations also show that the shock wave is a discontinuity in the flow field and that the properties of the gas change abruptly across it.

# SCHLIEREN APPARATUS



SCHEMATIC PLAN

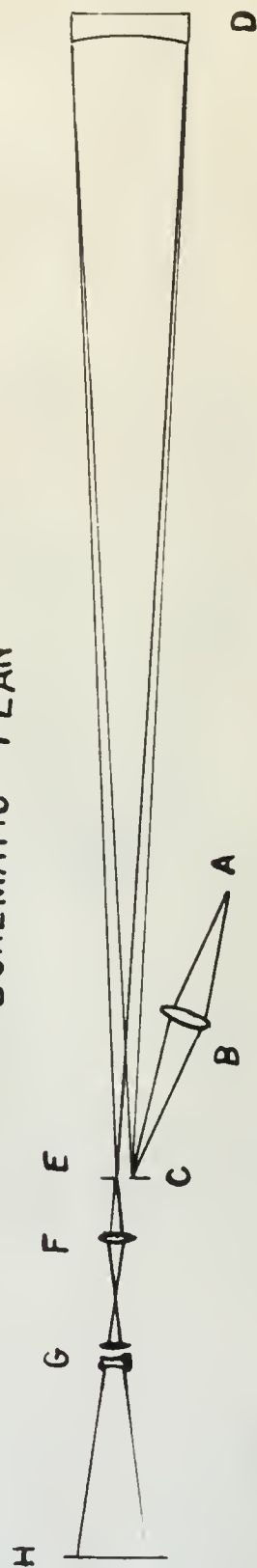


Fig. 1









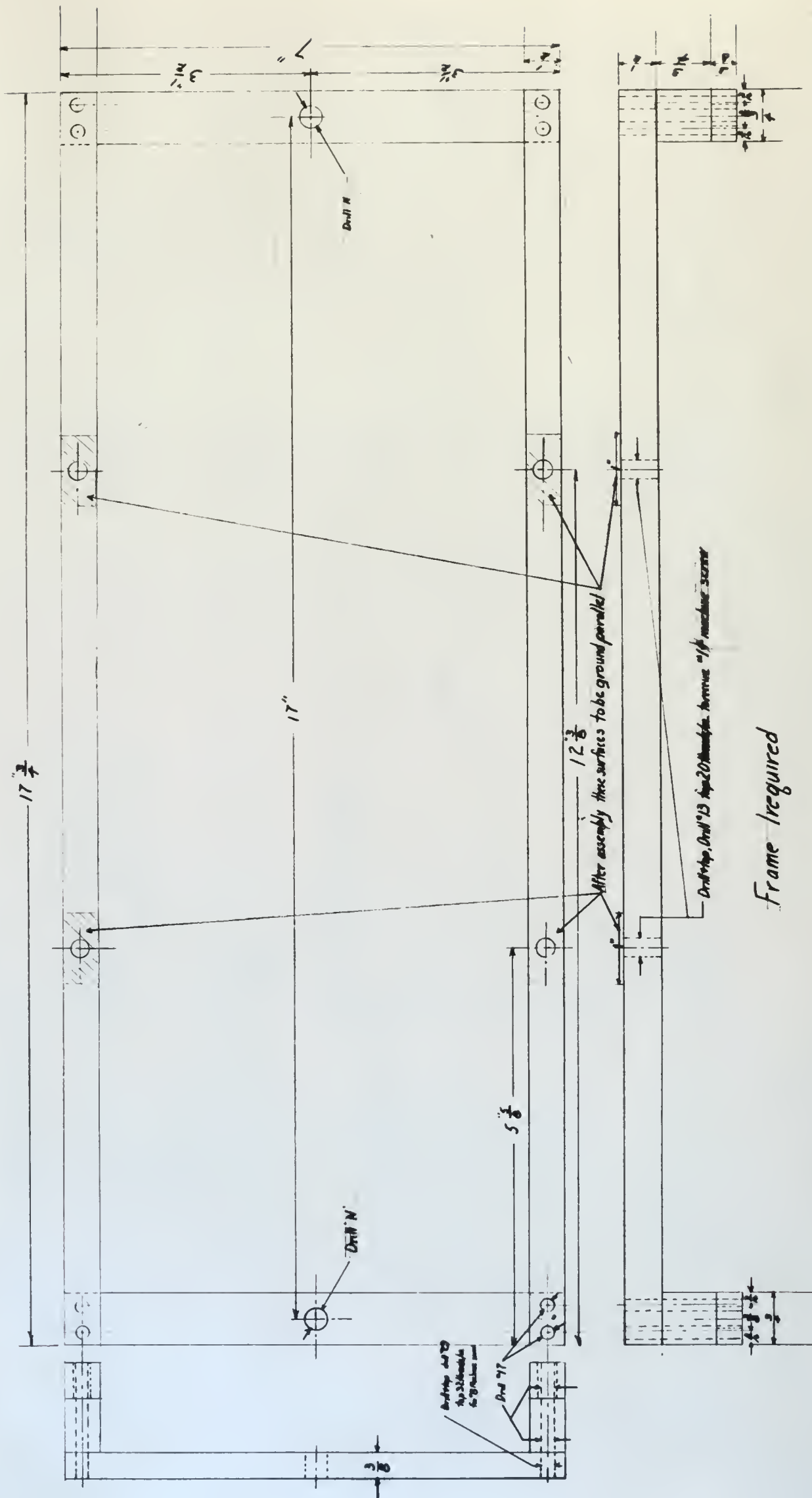
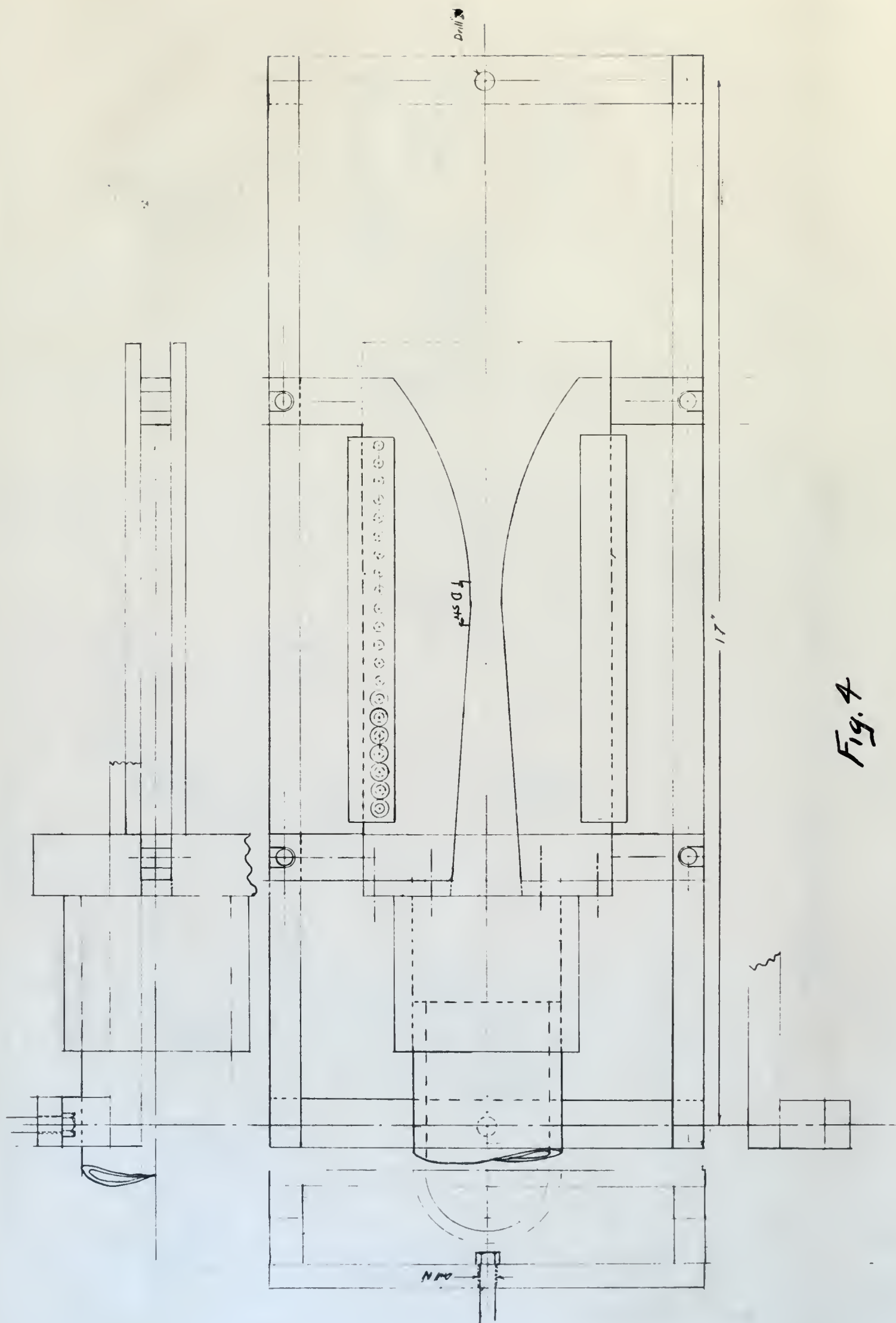


Fig. 3

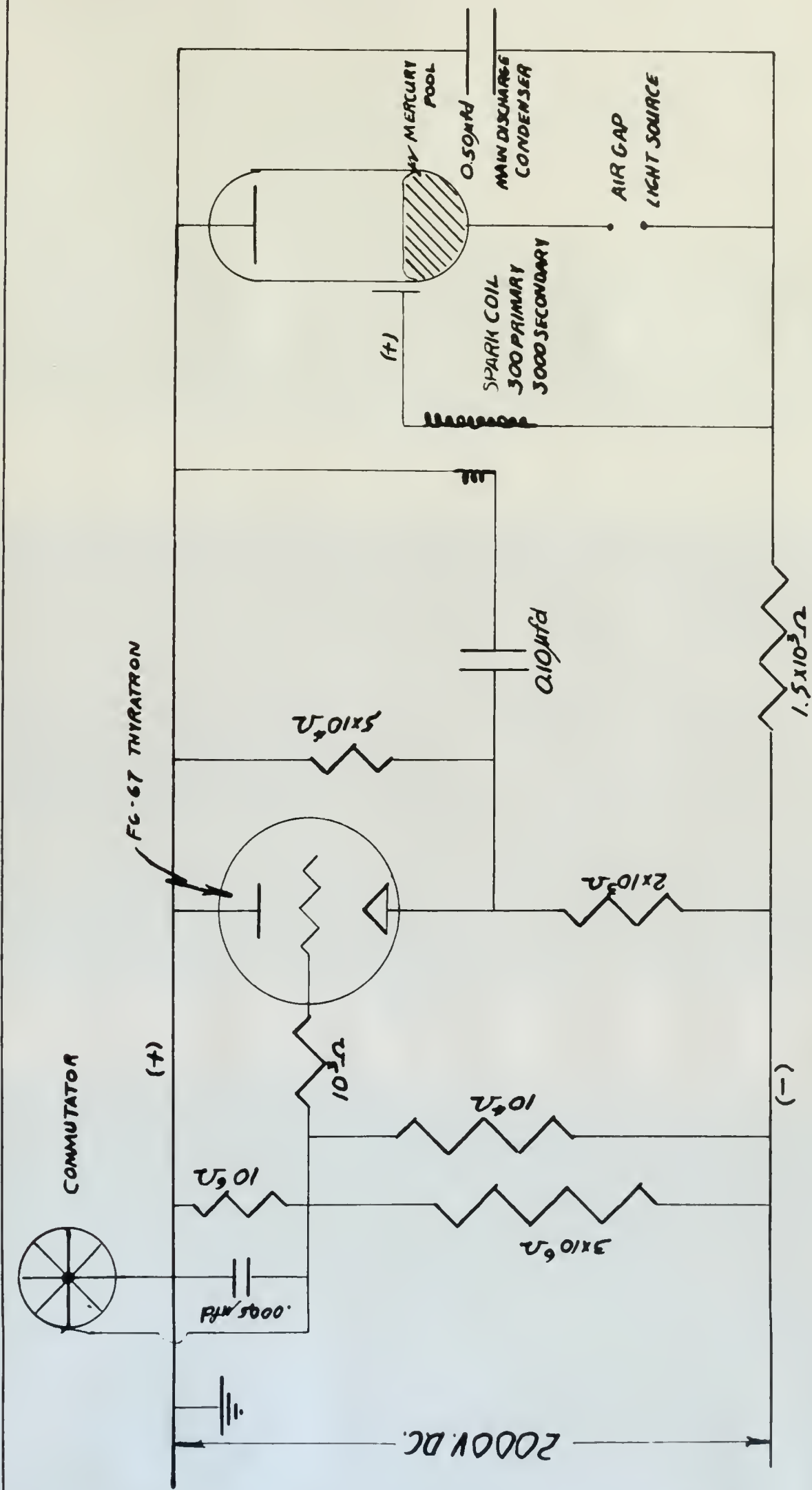












# Schematic Wiring Diagram of Light Source

Fig. 5



FIGS. 6 to 14.

SERIES 1.

TAKEN MAY 9, 1946, AT 3 P.M., AT M.I.T.  
PRESSURE RATIO, NOZZLE EXIT TO ENTRANCE, CONSTANT  
ENTRANCE PRESSURE, ATMOSPHERIC  
TIME INTERVAL BETWEEN PICTURES, ONE FIVE HUNDREDTH SECONDS  
EXPOSURE TIME, FIVE MICROSECONDS



FIG. 6 to 14.

SHINE I.

TAKEN MAY 9, 1946, AT 3 P.M., AT M.I.T.  
PRESSURE RATIO, MOISTURE RATIO TO SATURATION, CONSTANT  
SATURATION PRESSURE, TEMPERATURE  
TIME INTERVAL BETWEEN VIBRATIONS, ONE FIVE HUNDREDTHS SECONDS  
KILOPASCALS TIME, FIVE HUNDREDTHS



FIG. 6.



FIG. 7.



FIG. 8.







FIG. 9.



FIG. 10.



FIG. 11.





FIG. 12.



FIG. 13.





FIGS. 14 to 19.

SERIES 2.

TAKEN MAY 9, 1946, AT 3 P.M., AT M.I.T.  
PRESSURE RATIO, NOZZLE EXIT TO ENTRANCE, INCREASING  
ENTRANCE PRESSURE, ATMOSPHERIC  
TIME INTERVAL BETWEEN PICTURES, ONE FIVE HUNDREDTH SECONDS  
EXPOSURE TIME, FIVE MICROSECONDS

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FIG. 14.



FIG. 15.



FIG. 16.







FIG. 17.

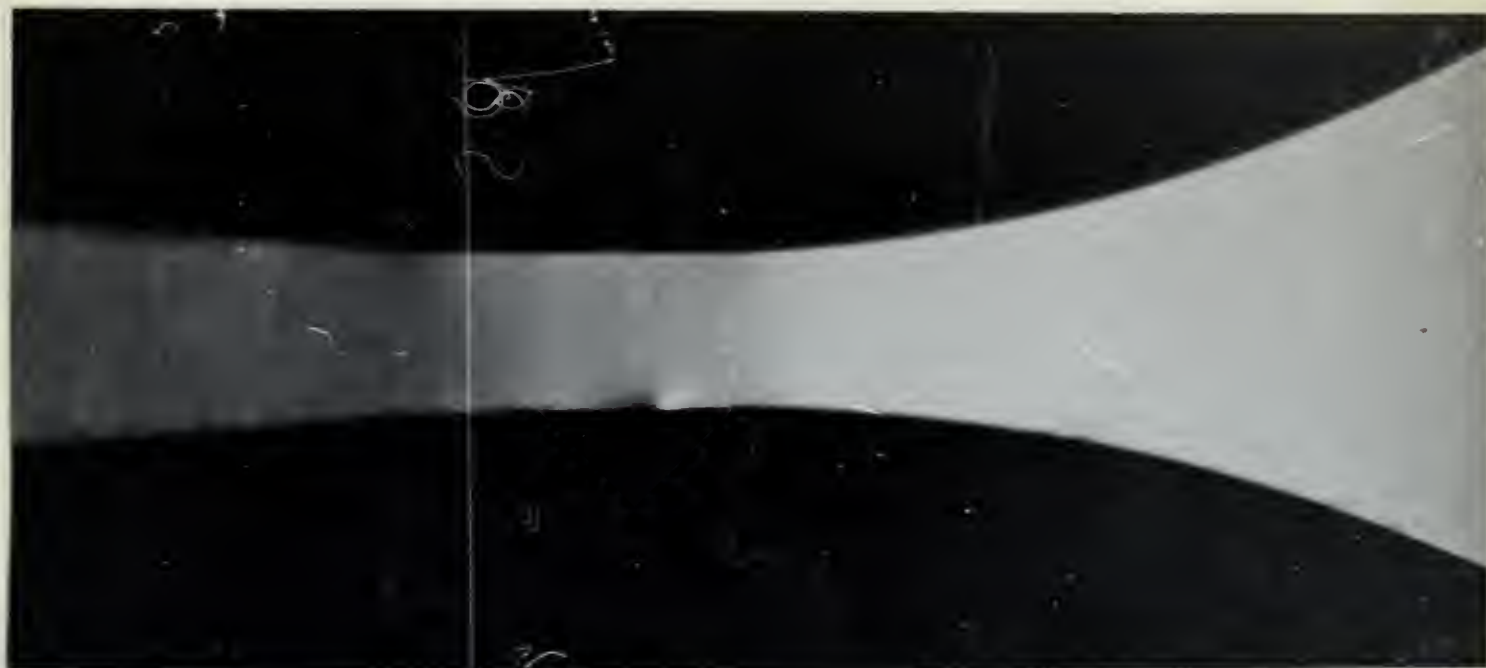


FIG. 18.



FIG. 19.



FIGS. 19 to 28.

SERIES 3.

TAKEN MAY 9, 1946, AT 3 P.M., AT M.I.T.  
PRESSURE RATIO, NOZZLE EXIT TO ENTRANCE, DECREASING  
ENTRANCE PRESSURE, ATMOSPHERIC  
TIME INTERVAL BETWEEN PICTURES, ONE FIVE HUNDREDTH SECONDS  
EXPOSURE TIME, FIVE MICROSECONDS

WINE 12 30 30.

WINE 3.

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SWAMP, SWAMP, SWAMP, SWAMP, SWAMP, SWAMP  
THE LAYAL SWAMP, SWAMP, SWAMP, SWAMP, SWAMP  
REPORTS THE, THE SWAMP, SWAMP, SWAMP, SWAMP, SWAMP





FIG. 20.



FIG. 21.



FIG. 22.





FIG. 23.

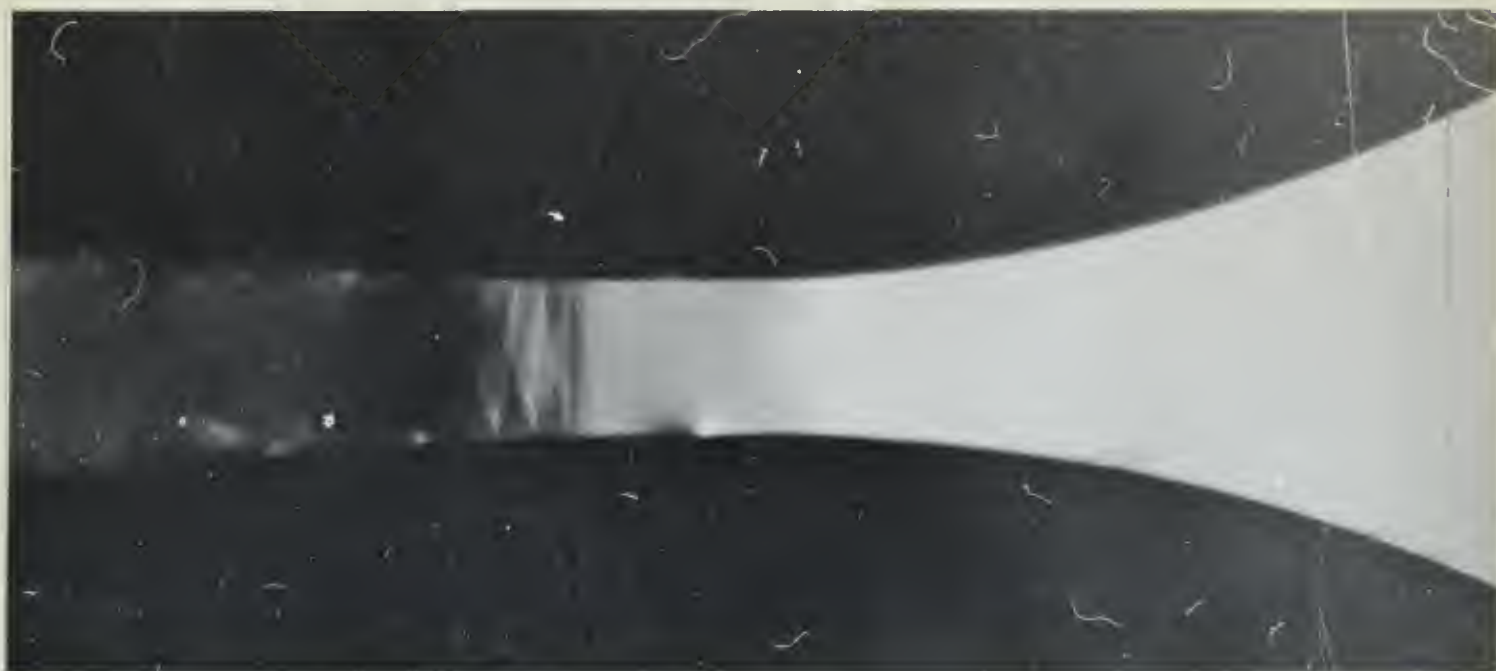


FIG. 24.



FIG. 25.





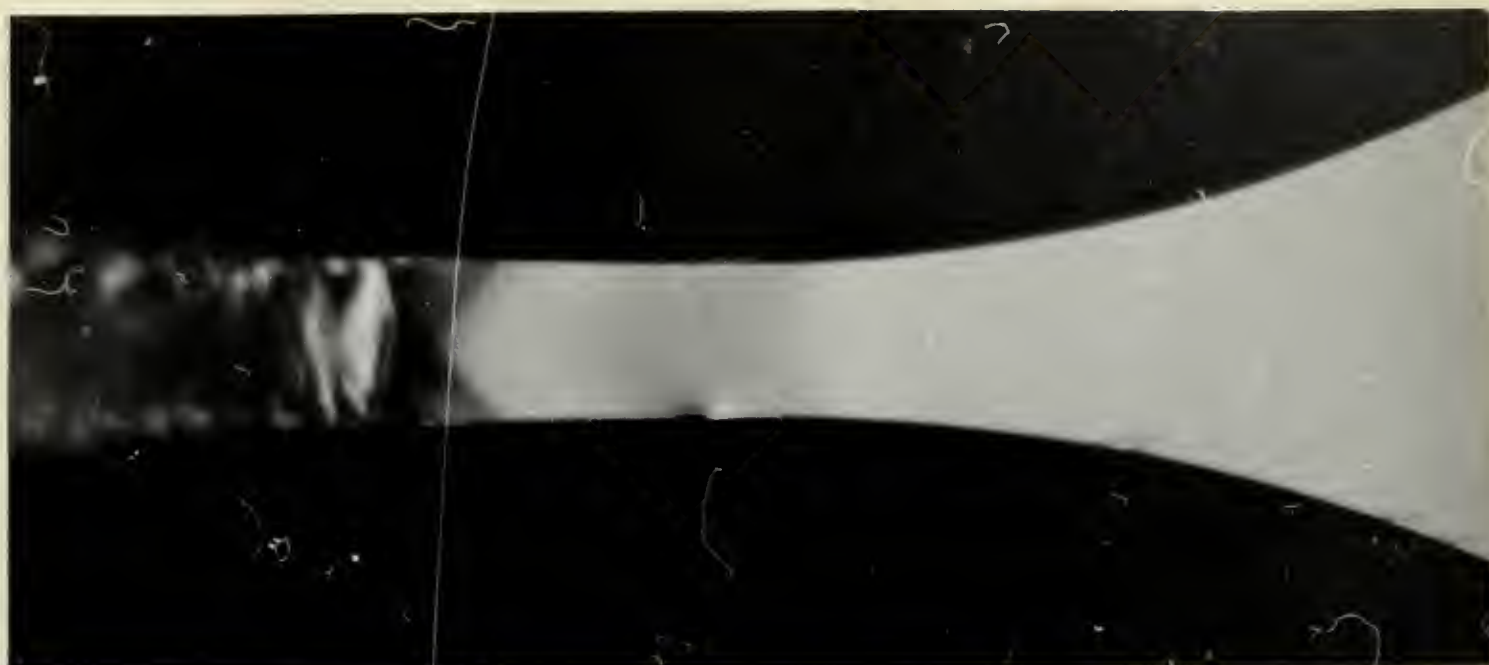


FIG. 26.



FIG. 27.



FIGS. 28 THROUGH 32.

TAKEN MAY 12, 1946, AT 10 A.M., AT M.I.T.  
PRESSURE RATIO, NOZZLE EXIT TO ENTRANCE, INCREASING  
ENTRANCE PRESSURE, ATMOSPHERIC  
EXPOSURE TIME, FIVE MICROSECONDS

Note: Pictures are not separated by constant time  
interval but are selected to show typical  
structures found.

[illegible]

1971  
The following are the names of the persons who have been  
involved in the work of the Committee since its formation  
in 1964.





FIG. 28.



FIG. 29.





FIG. 30.



FIG. 31.







FIG. 32



## APPENDIX I.

### DETAILED DESCRIPTION AND DISCUSSION OF APPARATUS.

#### THE SCHLIEREN EQUIPMENT

The Schlieren optical method was used to observe the phenomena investigated. The system used is sketched in Fig. 1. It consists essentially of a light source, a small plane mirror, a spherical concave mirror with a twenty-four foot focal length, a knife edge, a screen of ground glass, or photographic film, a system of corrected convex lenses, and the model to be observed.

Referring to Fig. 1, light is collected from the source "A", by the condensing lens "B", and focused on the small plane mirror "C". The point of focus is a point on the side of the plane mirror nearest the optical axis of the bench. A portion of the image of the source is allowed to pass between the mirror and the optical axis. This insures a sharp edge on the image cast back to the knife edge and permits accurate sensitivity adjustments. The light from the plane mirror is then cast through the test section on to the concave mirror "D". Thence the light is reflected back through the test section to the knife edge "E".

The knife edge is in the same plane as the plane mirror. This plane is located at one half the focal length of the mirror away from it, as measured along the optical axis. The

RELATIVE HUMIDITY AND LIQUIDITY OF AIR

THE RELATIVE HUMIDITY

The following optical method was used to observe the  
 phenomena investigated. The system used is sketched in  
 Fig. 1. It consists essentially of a light source, a small  
 plane mirror, a spherical convex mirror with a twenty-four  
 inch focal length, a knife edge, a system of ground glass,  
 or phase-contrast film, a system of horizontal screen lenses,  
 and the model to be observed.

Referring to Fig. 1, light is collected from the source  
 "A", by the condensing lens "B", and focused on the small  
 plane mirror "C". The point of focus is a point on the side  
 of the plane mirror nearest the optical axis of the model.

A position of the lamp of the source is allowed to pass  
 between the mirror and the optical axis. This causes a  
 sharp edge on the lamp cast back to the knife edge and pre-  
 sents a source readily adjustable. The light from the  
 plane mirror is then cast through the lens system on to the  
 screen mirror "D". Thence the light is reflected back  
 through the lens system to the knife edge "E".

The knife edge is in the same plane as the plane mirror.

This plane is inserted at one half the focal length of the  
 mirror away from it, as measured along the optical axis. The



knife edge is parallel to the edge of the mirror nearest the optical axis, so that light passing the knife edge appears as a sharply defined rectangular slit. The condensing lens "F" collects the light and the lens "G" focuses the light so that the test section is defined on the screen.

A decreasing density gradient toward the knife-edge side of the test section (downstream) causes a deflection of the rays passing through the test section away from the knife edge. An increasing pressure gradient in this direction refracts the light toward the knife edge. Thus, a decreasing density gradient in the direction of flow appears as a lighter region and an increasing one appears as a dark region.

A rotating table was used to mount the light source, so that the apparatus would be lined up and adjusted with a steady source; then pictures could be taken with the flash source by merely rotating the table.

The sensitivity is adjusted by moving the knife edge into or out of the beam of light reflected by the concave mirror, by means of a micrometer screw. Moving the knife edge into the beam increases the sensitivity. That is, smaller refractions of the light are blacked out on the viewing screen by the knife edge.

A complete discussion of the adjustments to the apparatus may be found in references (1) or (2).

knife edge is parallel to the edge of the mirror surface  
the optical axis, so that light passing the knife edge ap-  
pears as a sharply defined rectangular slit. The constant  
light intensity collected the light and the light intensity  
the light so that the light intensity is defined on the surface.  
A rectangular domain is defined across the knife-edge  
side of the light section (downstream) across a reflection  
of the light passing through the knife edge and the light  
knife edge. An interesting phenomenon is observed in this direc-  
tion towards the light towards the knife edge. When a  
decreasing intensity gradient in the direction of the surface  
as a linear region and an increasing one appears as a light  
region.

A rotating table was used to mount the light source,  
so that the experiment would be aimed up and rotated with a  
steady source; then distance could be taken with the plane  
source by merely rotating the table.  
The sensitivity is adjusted by rotating the knife edge  
into or out of the beam of light reflected by the rotating  
mirror, by means of a micrometer screw. Moving the knife  
edge into the beam increases the sensitivity. When it is  
similar variations of the light are observed out on the edge-  
ing towards the knife edge.  
A complete discussion of the adjustments to the experiment  
may be found in references (1) or (2).



### THE GLASS NOZZLE WALLS

The glass used on the sides of the nozzle had a large effect on the results obtained. First tried, was selected plate glass. This glass was high quality plate glass selected by means of an interferometer for flatness and parallelism of the planes. Selected points in each piece used were examined and at no place was a curvature of greater than thirty seconds of arc observed. However, when placed on the test section and observed through the apparatus, the effects of the glass were smaller but of the same order of magnitude as the compression shock which was under investigation. See Fig. A, Appendix I. Therefore, it was necessary to obtain two optically flat pieces of glass from which no glass effects could be observed through this apparatus. See Fig. 18.

Clamping stresses were avoided by holding the glass in place with cellulose tape. Pressure stresses were small because pressure differences were small, of the order of seven pounds per square inch, and the areas affected were small. The thickness of the glass used to obtain the final results totaled one inch, that is, each piece was one-half inch thick.

### THE HIGH SPEED MOVIE CAMERA

To obtain a series of pictures with a short time interval between pictures, a thirty-five millimeter, high speed

## THE GLASS WORKING

The glass was on the edge of the bottle and a large  
amount of the bottle collapsed. First tried, was selected  
glass plate. This glass was also quality glass and  
tested by means of an instrument for flatness and

parallelism of the glass. Coloured points in each glass  
used were examined and at no place was a variation of  
thickness than thirty seconds of the observed. However, when  
placed on the test machine and observed through the spec-  
tacle, the effects of the glass were similar to the same  
order of magnitude as the comparison made with the water  
instrument. See Fig. 4, Appendix I. Therefore, it was  
necessary to obtain the optical flat glass of glass from  
which no glass effects could be observed through this ap-

erture. See Fig. 14.

Optical stresses were avoided by holding the glass in  
place with oil-soluble tape. However, stresses were small  
because pressure differences were small at the point of  
stress points per square inch, and the glass allowed some  
small. The thickness of the glass used to obtain the final  
results totaled one inch, two is, each glass was one-half  
inch thick.

## THE AIR SPINNING METHOD

To obtain a series of pictures with a short time lag  
for between pictures, a thirty-five millimeter, six speed



camera was used. The camera consisted of two reels, one for unexposed film, and the other for winding the exposed film, and a sprocket guide wheel, all encased in a light tight box fitted with an exposure aperture. A motor drove the exposed film reel, and the sprocket wheel, turned by tension in the film from the exposed film reel, turned a commutator which actuated the light source. Frames were separated by the flashing light source. The camera and light source were capable of taking pictures at any rate of speed up to twelve hundred frames per second, the speed being controlled by a governor on the driving motor. Timing of the speed was effected by a sixty cycles per second spark at the edge of the film, leaving a blackened area on the edge of the film for each sixtieth of a second of time elapsed.

#### LIGHT SOURCES

The steady light source consisted of a filament electric lamp.

Several types of flashing sources were used. For the trial single pictures an "Edgerton Flash Tube" was used. This consists of a spark gap in an inert gas. The spark is corded, that is, it is made to pass through a glass tube of about one eighth inch inside diameter. The spark was about one and one-half inches long. (Ref. (2)).

For the high speed series of pictures the same type of tube was tried and found unsuccessful because the spark was





not corded into a narrow enough region. This motion of the spark caused the light to the plane mirror at times to be all on the mirror so that no definition of the edge of the mirror could be detected at the knife edge, hence losing control of the sensitivity adjustment, and at times to be completely off the plane mirror so that no light passed through the remainder of the system.

In an effort to reduce the wandering of the spark an air spark gap was tried, with no attempt made to cord the spark, but wandering of the spark materially reduced by reducing the length of the air gap to about one-quarter of an inch. This scheme was satisfactory but not excellent, since some variation in the density of the frames could be observed.

The mechanism for producing the spark is sketched diagrammatically in Fig. 5. An impulse from the commutator permitted the thyatron to pass current which in turn allowed the 0.10 microfarad condenser to discharge. This caused current to commence flowing in the primary of the spark coil which induced a voltage in the secondary. This voltage in the secondary was enough to "fire" the mercury tube and cause a breakdown across the air gap. Once the mercury tube commenced to pass electrons, the main discharge condenser, discharged across the air gap and through the mercury tube. The 1500 ohm resistor prevented firing of

not covered under a patent issued to the inventor. This device by the spark causes the light to the glass mirror at times to be all on the mirror as there is reflection of the light of the mirror could be detected at the light wave, hence, being control of the sensitivity adjustment, and as time to be completely off the glass mirror to that no light passed through the remainder of the system.

In an effort to reduce the amount of the spark as air space was used, with an attempt made to point the spark, but reduction of the spark actually reduced by reducing the length of the air gap to about one-quarter of an inch. This system was satisfactory but not excellent, since some variation in the density of the spark could be observed.

The mechanism for producing the spark is described electrically in Fig. 3. It isolates from the commutator generated the spark in such a way as to form a low 5.10 microsecond commutator in discharge. This caused current to pass through the primary of the spark coil which caused a voltage in the secondary. This voltage in the secondary was enough to "fire" the primary tube and cause a breakdown across the air gap. Once the primary tube commutator is gone, the spark, and the main discharge mechanism, is gone. The spark is produced by the primary tube. The 5.10 microsecond commutator is the spark.



the air gap once the main discharge condenser had discharged, but permitted this condenser to build up in voltage when no current was flowing through the air gap circuit. The rectifying nature of the mercury tube prevented a secondary spark from forming due to any inductance that probably existed in the actual main discharge circuit.

#### PHOTOGRAPHIC TECHNIQUE

It was found that the efficiency of the spark was materially reduced as to its effect on photographic plate when the spark was allowed to discharge through air rather than through an inert gas. Hence, in order to keep the exposure time short, it was found necessary to use the fastest obtainable movie film. It was not considered expedient to hypersensitize slower film due to the uncertainties involved, and the possible striations in the photographic film speed. The film used was Eastman Kodak Company's "Super XX".

In the development of the film it was found that maximum contrast could be obtained by chemically fogging the film very slightly. This merely ensured full development of all light struck portions of the exposed film. In order to do this the commercial developer "D-11" produced by Eastman Kodak Company was used and a developing time of sixteen minutes was used. The temperature of the developer was maintained as nearly at 68 degrees F. as possible to prevent excessive grain size in the negative.

the air got once the main discharge stream had been  
closed, but continued this movement to build up in  
pressure when no current was flowing through the air gap  
between the two electrodes. The resulting pressure of the vacuum tube pro-  
duced a secondary spark from the main gap as the latter  
was first partially closed in the second half cycle.

THE SECOND HALF CYCLE

It was found that the discharge at the start of  
the second half cycle was in the nature of a photoelectric flash  
when the spark was allowed to discharge through the vacuum  
tube through an inductance. Thus, in order to keep the dis-  
charge from being too large, it was found necessary to use the vacuum  
tube in the second half cycle. It was not considered expedient to  
operationalize the tube in the second half cycle as the acceleration involved,  
and the possible reactions in the discharge tube were  
the tube was found to be a vacuum tube.

In the experiment of the first half cycle it was found that the  
main discharge could be obtained by operating the vacuum tube  
in the second half cycle. This means that the vacuum tube  
of all these spark sources of the vacuum tube. In order  
to do this the vacuum tube of the vacuum tube was found  
to be a vacuum tube and a discharge tube of the vacuum tube  
was used. The vacuum tube of the vacuum tube was found  
to be a vacuum tube. It was found that the vacuum tube  
was also in the first half cycle.



### HEAT STRIATIONS

Heated wires were placed across the nozzle entrance parallel to the optical axis, in an effort to follow streamlines in the flow through the nozzle. However, these were found to disrupt the flow considerably and at maximum flow it was not feasible to heat the wires enough to follow the streamlines through the throat. It was feared that too much heat applied locally near the glass walls of the nozzle might break them. In obtaining the final results this scheme was abandoned.

### ADJUSTMENTS AFFECTING RESULTS

It was found that relatively small movements of the light source in a lateral direction caused shifts in the image which varied the sensitivity from "dark field" to no sensitivity at all. Movements of the order of a sixteenth of an inch from the mean were all that were necessary to provide this change in the position of the image relative to the knife edge. It was further found that motion of the light source of the same order of magnitude along the optical axis gave the same effect on the viewing screen due to motion of the focal point of the concave mirror relative to the knife edge.

It was found that when the glass walls of the test section were perpendicular to the optical axis reflections from the surfaces of the glass threw stray light into the screen that was not tolerable. Hence, all pictures are taken with

# THEORY OF THE

Healed after were placed under the double exposure  
parallel to the optical axis. In an effort to follow  
lines in the film through the mirror. However, these were  
found to disrupt the film considerably and at various times  
it was not possible to find the lines enough to follow and  
extensive changes were made. It was found that the  
most best applied locally near the glass walls of the mirror  
edges were best. In obtaining the final results this method  
was abandoned.

## EXPERIMENTAL PROCEDURE

It was found that relatively small movements of the  
film surface in a lateral direction caused errors in the  
image which varied the sensitivity from point to point  
in a systematic way. In order to avoid this a systematic  
of an area from the area were all that were necessary to  
provide this change in the position of the image relative to  
the mirror edge. It was further found that motion of the  
light source of the same order of magnitude along the optical  
axis gave the same effect on the viewing system and the motion  
of the focal point of the camera mirror relative to the mirror  
edge.

It was found that when the film was at the best pos-  
sible was perpendicular to the optical axis and the mirror  
the motion of the film through the light into the system  
that was not satisfactory. Hence, all distances are taken with



an angle of about four degrees between the optical axis and a perpendicular to the plane of the glass walls of the test section.

The interval between frames was taken at about one five-hundredth of a second because the spark source was more dependable at this slow speed, and because some experimental shots taken at higher speeds up to eleven hundred frames per second indicated that local movements of the shock occurred at much higher speeds. The camera would only handle one hundred foot lengths of film and at higher speeds, after allowing for the camera to steady on the set speed, too short a total time interval was left for the manual operation of the butterfly valve. It was thought that the sudden closure of the valve by automatic means might inject air inertia problems into an already complicated one. Therefore, the high speed series of pictures taken are not continuous; that is, when shown through a moving picture camera they do not show the movement of the multiple shocks relative to each other in a smooth continuous motion.

The negatives of the results have not been cut, so that each run remains intact as it was made. These negatives are presented with the original copy of this thesis to M.I.T.



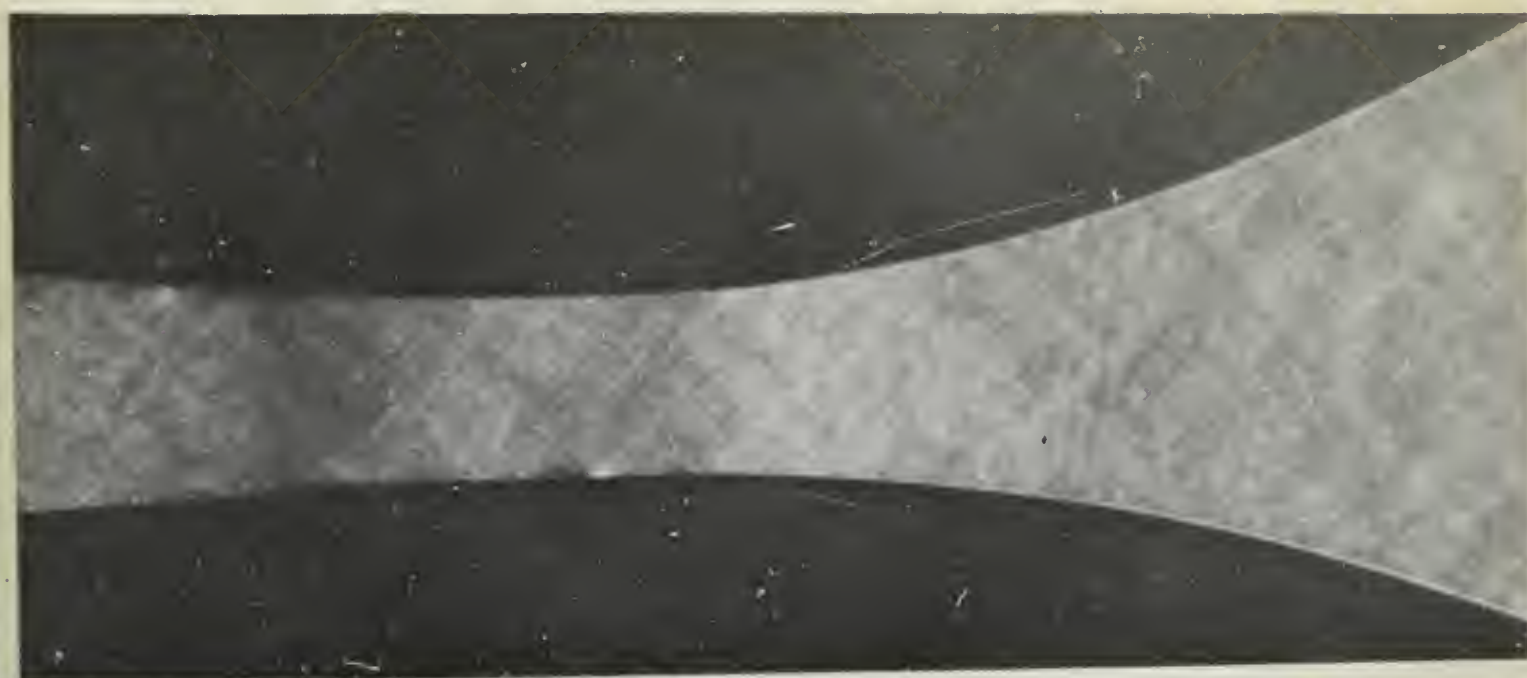


FIG. A.





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20.1.15, pp. 101-102.













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